## MOTION IN A PLANE

11th Standard CBSE

Reg.No. : $\square$
Exam Time : 01:00:00 Hrs

If $\overrightarrow{a_{1}}$ and $\overrightarrow{a_{2}}$ are two non collinear unit vectors and if $\left|\overrightarrow{a_{1}}+\overrightarrow{a_{2}}\right|=\sqrt{3}$, then the value of $\left(\overrightarrow{a_{1}}-\overrightarrow{a_{2}}\right) \cdot\left(\begin{array}{c}\overrightarrow{a_{1}}+\overrightarrow{a_{2}}\end{array}\right)$ is
(a) 2
(b) $\frac{3}{2}$
(c) $\frac{1}{2}$
(d) 1
2) The sum of magnitudes of two forces acting at a point is 18 units and the magnitude of their resultant is 12 units. The resultant is at $90^{\circ}$ with the force of the smaller magnitude. The magnitude of the individual forces is
(a) 5,12
(b) 5, 13
(c) 6,14
(d) none of these
3)

If the resultant of three forces $\vec{F}_{1}=p \hat{i}+3 \hat{j}-\hat{k}, \vec{F}_{2}$ and $\vec{F}_{3}=6 \hat{i}-\hat{k}$ acting on a particle has a magnitude equal to 5 units, then the value of p is
(a) -6
(b) -4
(c) 3
(d) 4
4) A vector is of magnitude $10 \sqrt{3}$ units and making equal angles with the positive direction of $x, y$ and $z$ axis is
(a) ${ }^{10}(\hat{i}+\hat{j}+\hat{k})$
(b) ${ }^{10}(\hat{i}+2 \hat{j}+3 \hat{k})$
(c) ${ }^{10}(\hat{i}-\hat{j}-\hat{k})$
(d) $10(\hat{i}-\hat{j}+\hat{k})$
5) A body is projected horizontally with a velocity of $4 \mathrm{~ms}^{-1}$. The velocity of the body after 0.7 s is nearly (take $\mathrm{g}=10 \mathrm{~ms}=-2$ )
(a) $10 \mathrm{~ms}^{-1}$
(b) $8 \mathrm{~ms}^{-1}$
(c) $19.2 \mathrm{~ms}^{-1}$
(d) $11 \mathrm{~ms}^{-1}$
${ }^{6)}$ A particle moves on a given line with a constant speed $v$. At a certain time it is at a point P on its straight line path. O is fixed point. The value of $\overrightarrow{O P} \times \vec{v}$ is (where y is perpendicular distance from O to given line)
(a) $-\mathrm{y} v \hat{k}$
(b) $-2 \mathrm{y} v \hat{k}$
(c) $-3 \mathrm{y} v \hat{k}$
(d) none
7) From the top of a tower of height 40 m , a ball is projected upwards with a speed of $20 \mathrm{~m} / \mathrm{s}$ at an angle of elevation of $30^{\circ}$. The ratio of the total time taken by the ball to hit the ground to its time of flight (time taken to come back to the same elevation) is (Take $g=10 \mathrm{~m} / \mathrm{s}^{2}$ )
(a) $2: 1$
(b) $3: 1$
(c) $3: 2$
(d) $1.5: 1$
${ }^{8)}$ A boy aims a gun at a target from a point, at a horizontal distance of 100 m . if the gun can impart a horizontal velocity of $500 \mathrm{~ms}^{-1}$ to the bullet, the height above the target where he must aim his gun, in order to hit it is (Take $\mathrm{g}=10 \mathrm{~ms}^{-2}$ )
(a) 20 cm
(b) 10 cm
(c) 50 cm
(d) 100 cm
${ }^{9)}$ At the top of the trajectory of a projectile, the directions of its velocity and accelerations are

Choose the correct option/s.
(a) To represent two-dimensional motion we need vectors
(b) To represent one-dimensional motion we use positive and negative signs
(c) To represent 3-dimensional motion we need vectors
(d) All (a), (b) and (c)
17) $|\lambda \mathbf{A}|=\lambda|\mathbf{A}|$, if
(a) $\lambda>0$
(b) $\lambda<0$
(c) $\lambda=0$
(d) $\lambda \neq 0$
18) If $A$ is a vector with magnitude IAI, then the unit vector it in the direction of vector $A$ is
(a) AA
(b) $A \cdot A$
(c) AxA
(d) $\frac{\mathbf{A}}{|\mathbf{A}|}$
19) Given $|\mathbf{A}+\mathbf{B}|=P,|\mathbf{A}-\mathbf{B}|=0$ The value of $\mathrm{p}^{2}+\mathrm{Q}^{2}$ is
(a) $2\left(\mathrm{~A}^{2}+\mathrm{B}^{2}\right)$
(b) $\mathrm{A}^{2}-\mathrm{B}^{2}$
(c) $A^{2}+B^{2}$
(d) $2\left(\mathrm{~A}^{2}-\mathrm{B}^{2}\right)$
20) Choose the correct option regarding the given figure.

(a) $\mathrm{B}=\mathrm{A}$
(b) $\mathrm{B}=-\mathrm{A}$
(c) I B I = I A I
(d) $|\mathbf{B}| \neq|\mathbf{A}|$
21) In a two dimensional motion, instantaneous speed $V_{o}$ is a positive constant. Then, which of the following are necessarily true?
(a) The acceleration of the particle is zero
(b) The acceleration of the particle is bounded
(c) The acceleration of the particle is necessarily in the plane of motion
(d) The particle must be undergoing a uniform circular motion
${ }^{22)}$ Figure shows the orientation of two vectors $u$ and $v$ in the xy-plane


If $\mathbf{u}=a \hat{\mathbf{i}}+b \hat{\mathbf{j}}$ and $\mathbf{v}=p \hat{\mathbf{i}}+q \hat{\mathbf{j}}$ Which of the following is correct?
(a) a and p are positive while band q are negative
(b) a, p and b are positive while q is negative
(c) $\mathrm{a}, \mathrm{q}$ and b are positive while p is negative
(d) a, b, p and q are all positive
23) A man standing on a road has to hold his umbrella at $30^{\circ}$ with the vertical to keep the rain away. He throws the umbrella and starts running at $10 \mathrm{kmh}^{-1}$. He finds that raindrops are hitting his head vertically. The actual speed of raindrops is
(a) $20 \mathrm{kmh}^{-1}$
(b) $10 \sqrt{3} \mathrm{kmh}^{-1}$
(c) $20 \sqrt{3} \mathrm{kmh}^{-1}$
(d) $10 \mathrm{kmh}^{-1}$
24) Three particles A, Band C projected from the same point with the same initial speeds making angle $30^{\circ}, 45^{\circ}$ and $60^{\circ}$, respectively with the horizontally. Which of the following statements is correct?
(a) A, B and C have unequal ranges
(b) Ranges of A and C are less than that of B
(c) Ranges of A and C are equal and greater than that of B
(d) A, Band C have equal ranges

The ceiling of a hall is 30 m high. A ball is thrown with $60 \mathrm{~ms}^{-1}$ at an angle $\theta$, so that maximum horizontal distance may be covered. The angle $\theta$ of projection is given by
(a) $\sin \theta=\frac{1}{\sqrt{8}}$
(b) $\sin \theta=\frac{1}{\sqrt{6}}$
(c) $\sin \theta=\frac{1}{\sqrt{3}}$
(d) None of these
26)

Two cars of masses $m_{1}$ and $m_{2}$ are moving in circles of radii $r_{1}$ and $r_{2}$ respectively. Their speeds are such that they make complete circles in the same time $t$. The ratio of their centripetal accelerations is
(a) $\mathrm{m}_{1} \mathrm{r}_{1}: \mathrm{m}_{2} \mathrm{r}_{2}$
(b) $\mathrm{m}_{1}: \mathrm{m}_{2}$
(c) $\mathrm{r}_{1}: \mathrm{r}_{2}$
(d) $1: 1$
${ }^{27)}$ In a two dimensional motion, instantaneous speed $V_{o}$ is a positive constant. Then, which of the following are qecessarily true?
(a) The average velocity is not zero at any time (b) Average acceleration must always vanish
(c) Displacements in equal time intervals are equa
(d) Equal path lengths are traversed in equal intervals
${ }^{28)}$ A particle starts from origin at $t=0$ with a velocity $5.0 \hat{\mathrm{i} m s}{ }^{-1}$ nd moves in XY-plane under action of force which produces a constant acceleration of $(3.0 \hat{\mathbf{i}}+2.0 \hat{\mathbf{j}}) \mathrm{ms}^{-2}$. What is the $y$-coordinate of the particle at the instant when its x -coordinate is 84 m ?
(a) 36 m
(b) 24 m
(c) 39 m
(d) 18 m
${ }^{29)}$ Two projectiles $A$ and $B$ thrown with speeds in the ratio $1: \sqrt{2}$ acquired the same height. If $A$ is thrown at an angle of $45^{\circ}$ with the horizontal, then angle of projection of $B$ will be
(a) $0^{\circ}$
(b) $60^{\circ}$
(c) $30^{\circ}$
(d) $45^{\circ}$
30) If a person can throw a stone to maximum heiqht of $h$ metre vertically, then the maximum distance through which it can be thrown horizontally by the same person is
(a) $\frac{h}{2}$
(b) h
(c) 2 h
(d) 3 h
${ }^{31)}$ The displacement of a particle moving on a circular path of radius T when it makes $60^{\circ}$ at the centre is
(a) 2 r
(b) r
(c) $\sqrt{2} r$
(d) None of these
${ }^{32)}$ What is the position vector of a point mass moving on a circular path of radius of 10 m with angular frequency of 2 rads $^{-1}$ after $\pi / 8 \mathrm{~s}$. Initially the point was on Y -axis.
(a) $5 \cdot(\hat{\mathbf{i}}+\hat{\mathbf{j}})$
(b) $5 \sqrt{2}(\hat{\mathbf{i}}+\hat{\mathbf{j}})$
(c) $\hat{\mathbf{i}}+\hat{\mathbf{j}}$
(d) $\frac{1}{\sqrt{2}}(\hat{\mathbf{i}}+\hat{\mathbf{j}})$
33) The angle between $\mathbf{A}=\hat{\mathbf{i}}+\hat{\mathbf{j}}$ and $\mathbf{B}=\hat{\mathbf{i}}-\hat{\mathbf{j}}$ is
(a) $45^{\circ}$
(b) $90^{\circ}$
(c) $-45^{\circ}$
(d) $180^{\circ}$
34)

The quantities $A_{x}$ and $A_{y}$ are called $x$ and $y$ components of the vector $A$. Note that $A_{x}$ is itself not a vector, but $A_{x} \hat{\mathbf{i}}$ is a vector, and so is $A_{y} \hat{\mathbf{j}}$. Using simple trigonometry, we can express $A_{x}$ and $A_{y}$ in terms of the magnitude of A and the angle it makes with the x -axis
$\mathrm{A}_{\mathrm{x}}=\mathrm{A} \cos \theta$
$\mathrm{A}_{\mathrm{y}}=\mathrm{A} \sin \theta$
Choose the correct figure on the basis of given description.
(a)

(b)

(c)

(d) None of these
35)

The direction of instantaneous velocity is shown by
(a)

(b)

(c)

(d) None of these
${ }^{36)}$ girl riding a bicycle with a speed of $5 \mathrm{~ms}^{-1}$ towards North direction sees raindrops falling vertically downwards. On increasing the speed to $15 \mathrm{~ms}^{-1}$ rain appears to fall making an angle of $45^{\circ}$ of the vertical. Find the magnitude of velocity of rain.
(a) $5 \mathrm{~ms}^{-1}$
(b) $5 \sqrt{5} \mathrm{~ms}^{-1}$
(c) $25 \mathrm{~ms}^{-1}$
(d) $10 \mathrm{~ms}^{-1}$
37)

The speed of a projectile at the maximum height is $1 / 2$ its initial speed. Find the ratio of range of projectile to the maximum height attained.
(a) $4 \sqrt{3}$
(b) $\frac{4}{\sqrt{3}}$
(c) $\frac{\sqrt{3}}{4}$
(d) 6
38)

The horizontal range of a projectile fired at an angle of $15^{\circ}$ is 50 m . If it is fired with the same speed at an angle of $45^{\circ}$, its range will be
(a) 60 m
(b) 71 m
(c) 100 m
(d) 141 m
39)

Two cars A and B move along a concentric circular path of radius $r_{A}$ and $r_{B}$ with velocities $v_{A}$ and $\mathrm{v}_{\mathrm{B}}$ maintaining constant distance, the $\frac{v_{A}}{v_{B}}$ is equal to
(a) $\frac{r_{B}}{r_{A}}$
(b) $\frac{r_{A}}{r_{B}}$
(c) $\frac{r_{A}^{2}}{r_{B}^{2}}$
(d) $\frac{r_{B}^{2}}{r_{A}^{2}}$
40)

The length of seconds hand of a watch is 1 cm , The change in velocity of its tip in 15 seconds in $\mathrm{cm} / \mathrm{s}$ is
(a) zero
(b) $\frac{x}{(30 \sqrt{2})}$
(c) $\frac{\pi}{30}$
(d) $\frac{2 \pi}{(30 \sqrt{2})}$
${ }^{41)}$ Five equal forces of 10 N each are applied at one point and are all lying in one plane. If the angles between them are equal, the resultant of these forces will be
(a) Zero
(b) 10 N
(c) 20 N
(d) $10 \sqrt{2} \mathrm{~N}$

Angle that the vector $\vec{A}=2 \hat{i}+2 \hat{j}$ makes with y -axis is
(a) $\tan ^{-1}(3 / 2)$
(b) $\tan ^{-1}(2 / 3)$
(c) $\sin ^{-1}(2 / 3)$.
(d) $\cos ^{-1}(3 / 2)$
${ }^{43)}$ The simple sum of two forces acting at a point is 16 N and their sum is 8 N and its direction is perpendicular to the smaller force, then the forces are:
(a) 6 Nand 10 N
(b) 8 Nand 8 N
(c) 4 Nand 12 N
(d) 2 Nand 14 N
${ }^{44)}$ If a unit vector is represented by $\mathbf{0 . 5 \hat { \boldsymbol { i } }}+\mathbf{0} .8 \hat{\mathbf{j}}+\boldsymbol{c} \hat{\boldsymbol{k}}$ then the value of 'c' is
(a) 1
(b) $\sqrt{0.11}$
(c) $\sqrt{0.01}$
(d) $\sqrt{0.39}$
${ }^{45)}$ A projectile is hurled into air from a point on the horizontal ground at an angle with the vertical. If the air exerts a constant resistive force,
(a) the path of projectile will be parabolic path.
(b) the time of ascent will be eq ual to time of decent.
(c) the total energy of the projectile is not conserved
(d) at the highest point, the velocity of projectile is horizontal.
${ }^{46)}$ A cart moves with a constant speed along a horizontal circular path. From the cart, a particle is thrown up vertically with respect to the cart, the particle will,
(a) land outside the circular path.
(b) land somewhere on the circular path.
(c) follow a parabolic path
(d) follow an elliptical path.
47)

A ball is bouncing elastically with a speed $1 \mathrm{~m} / \mathrm{s}$ between walls of a railway compartment of size 10 m in a direction perpendicular to walls. The train is moving at a constant velocity of $10 \mathrm{~m} / \mathrm{s}$ parallel to the direction of motion of the ball. As seen from the ground,
(a) the direction of motion of the ball changes every 10 seconds
(b) speed of ball changes every 10 seconds.
(c) average speed of ball over any 20 second interval is fixed.
(d) the acceleration of ball is the same as from the train.
48)

Three vectors $\vec{A}, \vec{B}$ and $\vec{C}$ add up to zero. Find which is false
(a) $\vec{A}(\vec{B} \times \vec{C})$ is not zero unless $\vec{B}, \vec{C}$ are parallel.
(b) $\vec{A}(\vec{B} \times \vec{C})$ is zero unless $\vec{B}, \vec{C}$ are parallel.
(c) If $\vec{A}, \vec{B}, \vec{C}$ define a plane, $\vec{A} \times(\vec{B} \times \vec{C})$ is in that plane
(d) $\vec{A},(\vec{B}, \vec{C})=|\vec{A}\|\vec{B}\|| \vec{C} \mid \rightarrow C^{2}=A^{2}+B^{2}$
49)

It is found that $|\overrightarrow{\boldsymbol{A}}+\overrightarrow{\boldsymbol{B}}|=|\overrightarrow{\boldsymbol{A}}|$.This necessarily implies
(a) $\vec{B}=\overrightarrow{0}$
(b) $\vec{A}, \vec{B}$ are antiparallel.
(c) $\vec{A}, \vec{B}$ are perpendicular.
(d) $\vec{A}, \vec{B} \leq 0$
${ }^{50)}$ Two particles are projected in air with speed $V_{0}$ at angles $\theta_{1}$ and $\theta_{2}$ (both acute) to the horizontal, respectively. If the height reached by the first particle is greater than that of the second, then tick the right choices
(a) angle of projection: $\mathrm{q}_{1}>\mathrm{q}_{2}$
(b) Time of flight: $\mathrm{T}_{1}>\mathrm{T}_{2}$
(c) horizontal range: $\mathrm{R}_{1}>\mathrm{R}_{2}$
(d) total energy: $\mathrm{U}_{1}>\mathrm{U}_{2}$
${ }^{51)}$ A particle slides down a frictionless parabolic $\left(y=x^{2}\right)$ track $(A \rightarrow B \rightarrow C)$ starting from rest at point $A$ (Fig.). Point $B$ is at the vertex of parabola and point $C$ is at a height less than that of point A. After $C$, the particle moves freely in air as a projectile. If the particle reaches highest point at $P$, then
(a) KE at $\mathrm{P}=\mathrm{KE}$ at B .
(b) height at $\mathrm{P}=$ height at A
(c) total energy at $\mathrm{P}=$ total energy at A
(d) time of travel from A to $\mathrm{B}=$ time of travel from B to P .
52)

Following are four different relations about displacement, velocity and acceleration for the motion of a particle in general. Choose the incorrect one (s):
(a) $\overrightarrow{v_{a v}}=\frac{1}{2}\left[\vec{v}\left(t_{1}\right)+\vec{v}\left(t_{2}\right)\right]$
(b) $\overrightarrow{v_{a v}}=\frac{\vec{r}\left(t_{2}\right)-\vec{r}\left(t_{1}\right)}{t_{2}-t_{1}}$
(c) $\vec{r}=\frac{1}{2}\left[\vec{v}\left(t_{2}\right)+\vec{v}\left(t_{1}\right)\right]\left(t_{2}-t_{1}\right)$
(d) $\overrightarrow{a_{a v}}=\frac{\vec{v}\left(t_{2}\right)-\vec{v}\left(t_{1}\right)}{t_{2}-t_{1}}$
${ }^{53)}$ For a particle performing uniform circular motion, choose the correct statement(s) from the following:
(a) Magnitude of particle velocity (speed) remains constant.
(b) Particle velocity remains directed perpendicular to radius vector.
(c) Direction of acceleration keeps changing as particle moves.
(d) Angular momentum is constant in magnitude but direction keeps changing.
54) A body is thrown with a velocity of $10 \mathrm{~ms}^{-1}$ at an angle of $60^{\circ}$ with the horizontal. Its velocity at the highest point is
(a) zero
(b) $5 \mathrm{~ms}^{-1}$
(c) $10 \mathrm{~ms}^{-1}$
(d) $8.66 \mathrm{~ms}^{-1}$
${ }^{55)}$ A person moves 30 m North, then 20 m East then $30 \sqrt{2} \mathrm{~m}$ South-West. His displacement from the original position is
(a) 14 m South-West
(b) 28 m South
(c) 10 m West
(d) 15 m East
56) During projectile motion the quantities that remain unchanged are
(a) force and vertical velocity
(b) acceleration and horizontal velocity
(c) kinetic energy and acceleration
(d) acceleration and momentum
57)

A constant force is acting perpendicular to the velocity of a particle. For this situation which one is correct?
(a) Velocity is constant.
(b) Acceleration is constant
(c) Momentum will be constant
(d) Particle will follow elliptical path.
58) The $x$-component of the resultant of several vectors
(a) is equal to the sum of the x-cornponents of the vectors
(b) maybe equal to the sum of the magnitudes of the vectors.
(c) maybe smaller than the sum of the magnitude of the vectors.
(d) maybe greater than the sum of the magnitude of the vectors
59)

The angle between $\vec{A}=\hat{i}+\hat{j}$ and $\vec{B}=\hat{i}-\hat{j}$ is
(a) $45^{\circ}$
(b) $90^{\circ}$
(c) $-45^{\circ}$
(d) $180^{\circ}$
60)

For two vectors $\vec{A}$ and $\vec{B}$ and $\vec{B}|\vec{A}+\vec{B}|=|\vec{A}-\vec{B}|$ when:
(a) $|\vec{A}|=|\vec{B}| \neq 0$
(b) $\vec{A} \perp \vec{B}$
(c) $|\vec{A}|=|\vec{B}| \neq 0$ and $\vec{A}$ and $\vec{B}$ are parallel or anti parallel.
(d) When either $|\vec{A}|$ or $|\vec{B}|$ is zero.

1) (c) $\frac{1}{2}$
2) (b) 5, 13
3) 

(c) 3
4)
(a) ${ }^{10}(\hat{i}+\hat{j}+\hat{k})$
5)
(b) $8 \mathrm{~ms}^{-1}$
6) (a) $-y \nu \hat{k}$
7)
(a) $2: 1$
8)
(a) 20 cm
9)
(d) inclined to each other at an angle of $45^{\circ}$
10)
(b) $5 \sqrt{3}$
11)
(d) A scalar quantity has the same value for observers with different orientation of the axes
12)
(b) impulse
13)
(c) they have opposite directions
14)
(d)

15)
(b) $r$ is along positive $x$-axis
16)
(d) All (a), (b) and (c)
17) (a) $\lambda>0$
18)
(d) $\frac{\mathbf{A}}{|\mathbf{A}|}$
19)
(a) $2\left(A^{2}+B^{2}\right)$
20)
(d) $|\mathbf{B}| \neq|\mathbf{A}|$
21) (c) The acceleration of the particle is necessarily in the plane of motion
22)
(b) $\mathrm{a}, \mathrm{p}$ and b are positive while q is negative
23)
(a) $20 \mathrm{kmh}^{-1}$
24)
(b) Ranges of $A$ and $C$ are less than that of $B$
25)
(b) $\sin \theta=\frac{1}{\sqrt{6}}$
26)
(c) $r_{1}: r_{2}$
27)
(d) Equal path lengths are traversed in equal intervals
28)
(a) 36 m
29)
(c) $30^{\circ}$
30)
(c) 2 h
31)
(b) $r$
32)
(b) $5 \sqrt{2}(\hat{\mathbf{i}}+\hat{\mathbf{j}})$
33)
(b) $90^{\circ}$
34)
(a)

35)

36) (b) $5 \sqrt{5} \mathrm{~ms}^{-1}$
37)
(b) $\frac{4}{\sqrt{3}}$
38) (c) 100 m
39)
(b) $\frac{r_{A}}{r_{B}}$
40)
${ }^{41)}$ (a) Zero
42) (b) $\tan ^{-1}(2 / 3)$
43)
(a) 6 Nand 10 N
44)
(b) $\sqrt{0.11}$
45)
(a) the path of projectile will be parabolic path.
46)
(a) land outside the circular path.
47)
(b) speed of ball changes every 10 seconds.
48)
(c) If $\vec{A}, \vec{B}, \vec{C}$ define a plane, $\vec{A} \times(\vec{B} \times \vec{C})$ is in that plane
49)
(b) $\vec{A}, \vec{B}$ are antiparallel.
50)
(a) angle of projection: $q_{1}>q_{2}$
51)
(c) total energy at $\mathrm{P}=$ total energy at A
52)

$$
\text { (a) } \overrightarrow{v_{a v}}=\frac{1}{2}\left[\vec{v}\left(t_{1}\right)+\vec{v}\left(t_{2}\right)\right]
$$

53) 

(a) Magnitude of particle velocity (speed) remains constant.
54) (b) $5 \mathrm{~ms}^{-1}$

1
(c) 10 m West
56)
(b) acceleration and horizontal velocity
57)
(b) Acceleration is constant
58) (a) is equal to the sum of the $x$-cornponents of the vectors
59) (b) $90^{\circ}$
60)
(b) $\vec{A} \perp \vec{B}$

